Ferroelectric substrate effects on the magnetism, magnetotransport, and electroresistance of La_{0.7}Ca_{0.3}MnO_3 thin films on BaTiO_3


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La_{0.7}Ca_{0.3}MnO_3 optimally doped epitaxial films were grown on ferroelectric BaTiO_3 substrates. Electronic transport (magnetoresistance and electroresistance) and magnetic properties showed important anomalies in the temperature interval between 60 and 150 K, below the metal-insulator transition. Scanning probe microscopy revealed changes in BaTiO_3 surface morphology at those temperatures. La_{0.7}Ca_{0.3}MnO_3 thickness is a critical factor: 120-Å-thick films showed large anomalies sensitive to electric poling of the BaTiO_3, whereas the behavior of 150-Å-thick films is closer to that of the reference La_{0.7}Ca_{0.3}MnO_3 samples grown on SrTiO_3. We propose that, through inhomogenous strain and electric polarization effects, the ferroelectric substrate induces an inhomogenous spin distribution in the magnetic layer. This would imply the coexistence of in-plane and out-of-plane ferromagnetic patches in La_{0.7}Ca_{0.3}MnO_3, possibly interspersed with antiferromagnetic regions, as it has recently been theoretically predicted. Substrate poling effects are investigated, and a magnetoelectric coupling is demonstrated.

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I. INTRODUCTION

Most recent developments in oxide-based spintronics involve multiferroic materials and/or multiferroic heterostructures. However, the few known natural multiferrosics have drawbacks. Those, such as BiFeO_3, with high electric polarization present weak coupling between the electronic and magnetic degrees of freedom. High magnetoelectric coupling comes with low electric polarizations arising with magnetic ordering, as in TbMnO_3 and TbMnO_3 (Ref. 3). Artificial multiferroic heterostructures can combine optimal ferromagnetic (FM) and ferroelectric properties, especially for spin-dependent tunnel devices with functional oxide barriers. Given the excellent epitaxial growth of perovskite thin films, devices combining ferroelectric BaTiO_3 and FM manganites, e.g. La_{0.7}Ca_{0.3}MnO_3 or La_{0.7}Sr_{0.3}MnO_3 are very attractive. These complex oxides are prone to phase separation, and their interface with ferroelectrics has been shown to exhibit a rich phenomenology, both experimentally (including a novel proposal for a metal-insulator transition near the interface due to electrostatic doping) and theoretically. Substrate-induced strain is propagated to epitaxially grown heterostructures of piezoelectrics and ferromagnets, such as BaTiO_3 and manganites. As a result, the strain-sensitive magnetic/charge/orbital states of the manganite can be altered through the piezoelectric with an electric field or conversely the polarization/strain of the piezoelectric may change by acting on the magnetic state of the ferromagnet.

Numerous studies recognize the complexity and the interest of bulk BaTiO_3 as a substrate. These features result from the occurrence of two structural phase transitions below room temperature, implying changes in the magnitude and direction of the spontaneous electrical polarization vector within the unit cell. Thus, varying degrees of strain and electric field are exerted on the thin layers, and the way is open to further control them by application of an external electric field to the substrates. The discontinuities in resistivity and low field magnetization of 500-Å La_{0.7}Sr_{0.3}MnO_3 films on BaTiO_3 due to the substrate structural phase transitions have been studied in Ref. 12. Converse magnetoelectric effects with coefficients as high as 2.3 × 10^{-7} s/m have been reported for 400-Å films of La_{0.7}Sr_{0.3}MnO_3 on BaTiO_3 in Ref. 11. Recently, we have also explored the magnetic behavior of a very thin layer of La_{0.7}Ca_{0.3}MnO_3 on poled BaTiO_3 (Ref. 18), a system with a narrower bandwidth than La_{0.7}Sr_{0.3}MnO_3 (Ref. 19) and enhanced tendency to microphase separation where the presence of an antiferromagnetic (AFM) insulating state is more likely.

Our previous study focused on the appearance of anomalous magnetic hysteresis loops, so called Matteucci cycles, in a set of thin La_{0.7}Ca_{0.3}MnO_3/BaTiO_3 films. We interpreted these results in terms of the existence of two populations of magnetic moments: a majority which aligns in plane with the transport properties of La_{0.7}Ca_{0.3}MnO_3 since the metal-insulator (MI) transition, accompanying the paramagnetic-to-FM transition, is percolative in nature. In addition, substrate corrugation is expected to introduce new phenomenology related to enhanced phase separation at the micron length scale.
Here, we explore the temperature dependence of the magnetization and transport properties (resistivity, magnetoresistance, electroresistance) of thin La$_{0.7}$Ca$_{0.3}$MnO$_3$ films on ferroelectric BaTiO$_3$ and compare them with those of thicker La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ films and La$_{0.7}$Ca$_{0.3}$MnO$_3$ grown on SrTiO$_3$. We show that the structurally epitaxial thin La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ films become electrically (and magnetically) granular and exhibit behavior not compatible with uniform long-range FM order. We correlate the observed magnetic and transport behavior with temperature-dependent surface morphology changes of BaTiO$_3$ in the rhombohedral (R) phase. We propose that a fine-grained secondary corrugation, developing in the R phase of BaTiO$_3$, could even enhance AFM correlations in La$_{0.7}$Ca$_{0.3}$MnO$_3$, in agreement with recent predictions, which would increase the resistance of the layer.

II. EXPERIMENTAL

Thin films were prepared on unpoled BaTiO$_3$ (001) and SrTiO$_3$ (001) ($5 \times 5 \times 1$ mm$^3$) substrates by sputtering with a highly oxidizing plasma (3.4 mbar oxygen atmosphere) at temperatures (1173 K), well above the BaTiO$_3$ ferroelectric Curie point. We will refer to these samples as La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ and La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$, respectively. The deposition rate was very slow (around 1 nm/min) and strict annealing (1 h at 823 K in 1 bar of oxygen) and cooling (20 K/min) procedures were followed. Several highly comparable samples of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ were grown using the same growth conditions, with 120-, 150-, and 240-Å thickness. For this study, control samples of La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ with 120-Å thickness, grown along with La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$, were studied in detail for comparison. The properties of La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ samples grown under the same conditions reported in this paper are detailed in Ref. 22.

The La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples were exposed to various thermal and electrical treatments during the experiments. When required, sample poling was effected ex situ at room temperature by repeatedly running a ferroelectric switching cycle on the BaTiO$_3$ substrate by applying a sufficiently large quasi-de electric field (up to 500 kV/m) between the La$_{0.7}$Ca$_{0.3}$MnO$_3$ film and a silver electrode on the back side. The typical switching field at room temperature was found to be around 70–80 kV/m. Later on, each sample was thermally cycled to low temperature during the electrical transport and magnetization measurements. Thermal and electrical fatigue eventually leads to cracking and loss of reproducibility in the measurements, at which point the damaged samples were discarded.

X-ray diffraction and reflectometry characterization of the La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ and La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ were performed on a Bruker D8 4-circle diffractometer (Cu K$_{α1}$ radiation) equipped with a LynxEye position sensitive detector. Also, BaTiO$_3$ substrates were studied at low temperatures using a bespoke cryogenic sample holder.

Temperature-dependent surface morphology was studied with scanning probe microscopy (SPM). Low-temperature SPM measurements were performed with a commercial system from Nanomagnetics Instruments and silicon cantilevers from BudgetSensors (Multi75Al-G). Amplitude modulation mode was used to investigate BaTiO$_3$ morphology as the temperature was decreased from 300 to 100 K. Topographic images were recorded (at a rate of 30 min/image) every 30 K (thermal stabilization periods of 60 min were allowed at each temperature) following the same area throughout the whole temperature range.

The temperature- and magnetic-field-dependent magnetization were measured using a vibrating sample magnetometer (VSM) or, alternatively, a superconducting quantum interference device (SQUID) magnetometer, both from Quantum Design, and equipped with 9- and 5-T coils, respectively. In the VSM measurements, 2-mm vibration amplitude at 40 Hz was used, whereas in SQUID magnetometry, the scan length was 3 cm. The temperature-dependent magnetization was measured following zero field cooling (ZFC, 10- and 100-mT measuring fields) and field cooling (FC, 10- and 100-mT cooling and measuring fields) protocols, the field being always in the plane of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ film. The magnetization is reported as magnetic moment per Mn ion of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ films in Bohr magnetons ($\mu_B$/Mn). The bulk saturation value in La$_{0.7}$Ca$_{0.3}$MnO$_3$ is 3.7 $\mu_B$/Mn. Magnetization hysteresis loops were recorded at various temperatures, after cooling to 10 K in 1 T, between ±1 T with a slow sweep rate of 1–2 mT/s. The diamagnetic contribution of the substrates was subtracted by estimating the high field linear dependence above the saturating field of La$_{0.7}$Ca$_{0.3}$MnO$_3$.

Electronic transport of the samples was characterized by measuring the resistance of the film in plane with the van der Pauw method, with contacts placed in the four corners of the square shaped samples. Voltage was measured with alternating direction of the dc excitation current to eliminate thermoelectric voltages. Furthermore, readings were taken quas simultaneouly, with the excitation current passing along one or the other perpendicular edges of the sample, parallel or perpendicular to the applied magnetic field. Magnetoresistance (MR) was calculated by normalizing to the zero-field resistance. Electroresistance (ER) was calculated from the nonlinear I-V curves. In order to discern and eliminate Joule-heating effects, at a few temperatures, pulsed I-V curves were recorded.

III. RESULTS

A. Structure and morphology

We have previously$^{18}$ reported structural results as a function of temperature for La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples exhibiting exotic Matteucci-like behavior obtained from coplanar and grazing incidence x-ray diffraction (GIXD) synchrotron studies. We found good epitaxial adherence of La$_{0.7}$Ca$_{0.3}$MnO$_3$ to BaTiO$_3$ in spite of the complexity of the
substrate, with $La_{0.7}Ca_{0.3}MnO_3$ lattice constants following consistently the changes experienced by BaTiO$_3$ at low temperature. In this paper, we report results obtained at low temperatures by x-ray diffraction and SPM on unpoled BaTiO$_3$ substrates. At room temperature, we extend our structural characterization with measurements of reciprocal space maps of coplanar symmetric and asymmetric reflections on $La_{0.7}Ca_{0.3}MnO_3$/BaTiO$_3$ and $La_{0.7}Ca_{0.3}MnO_3$/SrTiO$_3$.

1. Evolution with temperature of the ferroelectric domains and surface morphology of BaTiO$_3$

Although some debate still exists on the crystallographic description of the low-temperature phases of BaTiO$_3$ (Refs. 23 and 24), in this paper, we adopt the standard description as given, for example, in Ref. 25, which is closer to our observations. BaTiO$_3$ is cubic and paraelectric above 393 K. At room temperature, the tetragonal lattice parameters of BaTiO$_3$ are $a = b = 3.994$ Å and $c = 4.038$ Å. Upon cooling, at $T = 295$ K, BaTiO$_3$ undergoes a tetragonal (T) to orthorhombic (O) transition, and at $T = 183$ K, the system becomes R. The pattern of ferroelectric domains generated by the electric and elastic balance is modified by thermal cycles and/or poling, resulting in samples composed of misoriented twins. Thus, surface morphology changes and different corrugations are expected in all BaTiO$_3$ ferroelectric phases. We observe that repeated thermal or electrical poling eventually leads to fracture of our samples, which has been interpreted on the basis of local defect symmetry failing to adjust to long-range crystal symmetry.26,27

Figure 1 illustrates the evolution with temperature of the reflections arising from the ferroelectric domains of an unpoled BaTiO$_3$ substrate. Figure 1(a) corresponds to a reciprocal space map at room temperature near the tetragonal $(200) + (002)$ region. In this case, the sample was aligned with the reflection from the $a$ domain28 (out-of-plane lattice parameter: 3.995 Å), which appears as an intense peak near $L = 2$. Weaker peaks from $c$ domains are visible for $L = 1.976$, the maximum misorientation among them being 1.2°. Figure 1(b) shows the domain pattern in the orthorhombic phase taken at 200 K. The pattern resembles that observed in the tetragonal phase but with misorientations slightly smaller (0.5° for the value corresponding to pseudo-$c$ and pseudo-$a$ domains). Finally, in Fig. 1(c), taken at 77 K in the R phase, only two peaks of almost equal intensity are apparent. Their relative misorientation is 0.27°. Table I summarizes these results, together with the measured lattice parameters, which are in good agreement with the high-resolution neutron, low-strain, powder diffraction results from Ref. 25.

BaTiO$_3$ substrates exhibit great variability in their domain patterns due to the strong influence of thermal and electrical history. A representative unpoled (001) single crystal BaTiO$_3$ substrate was studied at various temperatures, upon cooling, with SPM in a low-pressure (10 Torr) He atmosphere. Topographic images of the same area are shown in Fig. 2 for selected temperatures at 300 K [Fig. 2(a)], 270 K [Fig. 2(b)], 180 K [Fig. 2(c)], and 100 K [Fig. 2(d)]. To better highlight possible changes in morphology with temperature, line profiles are compared in pairs in Figs. 2(e)–2(g). In order to avoid image processing artifacts, only global plane subtraction was applied prior to profile measurement. The corresponding morphology for the T, O, and R phases is shown in Figs. 2(a)–2(c). The surface morphology at 100 K is also presented in Fig. 2(d). In the scanned area, the BaTiO$_3$ surface exhibits, in all ferroelectric phases, a primary corrugation with a characteristic length around 15 μm that yields a mean roughness of 7.5 nm on 50 × 50 μm$^2$ areas. This corrugation, explained by the ferroelectric equilibrium conditions prevailing in the T phase,28 dominates the landscape, but some rippling of the slopes is also apparent. From 300 to 180 K, only minor

<table>
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<th>$T$ (K)</th>
<th>$a$ (Å)</th>
<th>$c$ (Å)</th>
<th>Misorientation angle (°)</th>
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<td>300</td>
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<td>4.038</td>
<td>0.6</td>
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<tr>
<td>200</td>
<td>4.019</td>
<td>3.991</td>
<td>0.5</td>
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<tr>
<td>77</td>
<td>4.005</td>
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FIG. 1. (Color online) Reciprocal space maps of an unpoled BaTiO$_3$ substrate cooled from (a) the tetragonal phase at room temperature to (b) the orthorhombic phase at 200 K, and finally to (c) the R phase at 77 K. The maps correspond to the region near (002) + (200) in the tetragonal phase and were taken by reference to a tetragonal (200) reflection.
changes are observed in the surface morphology corresponding to this dominant corrugation, which translate into very similar profiles for 300 and 270 K [Fig. 2(e)]. This behavior has also been reported in BaTiO₃ (111) samples studied by transmission electron microscopy.²⁸ At 180 K, differences are hardly noticeable in the SPM image, but line profiles show subtle deviations from those measured at higher temperatures [Fig. 2(f)]. These differences are marked with black arrows and show the disruption of the primary slope and the formation of a moundlike structure or secondary corrugation, with a characteristic length close to 7.5 µm, about half of value of the primary corrugation. In view of the variability exhibited by the BaTiO₃ substrates, the precise values of the corrugation characteristic lengths should not be understood as general properties of these ferroelectric substrates. The T-O structural phase transition at 295 K seems to trigger the observed changes in surface morphology, but it is below the O-R transition where the secondary corrugation consolidates. No further structural transition is expected on cooling below 183 K. Surprisingly, significant changes in the topographic profiles are measured at 100 K. These are marked in Fig. 2(g) and include height differences of up to 4 nm (over 2 µm) and the final formation of the secondary corrugation.

2. X-ray diffraction studies of La₀.₇Ca₀.₃MnO₃/SrTiO₃ and La₀.₇Ca₀.₃MnO₃/BaTiO₃ at room temperature

Figure 3 shows reciprocal space maps for a La₀.₇Ca₀.₃MnO₃/SrTiO₃ sample [Figs. 3(a) and 3(b)] and an unpoled La₀.₇Ca₀.₃MnO₃/BaTiO₃ sample [Figs. 3(c) and 3(d)] with 120-Å thickness as determined by x-ray reflectometry. At room temperature, SrTiO₃ has a cubic perovskite unit cell with parameter a = 3.905 Å. La₀.₇Ca₀.₃MnO₃ on SrTiO₃ [Fig. 3(a)] is epixtal with large spatial coherence, as evidenced by the peak width in the H direction. The observed out-of-plane La₀.₇Ca₀.₃MnO₃ lattice parameter is 3.824 Å. The in-plane lattice parameter of La₀.₇Ca₀.₃MnO₃ is that of SrTiO₃, as obtained from the asymmetric (-103) reflection [Fig. 3(b)]. The degree of relaxation, \( R = (a_h - a_s)/(a_p - a_s) \) with \( a_h \) the layer in-plane parameter, \( a_p \) the parameter in the bulk, and \( a_s \) the substrate in-plane parameter, is zero for La₀.₇Ca₀.₃MnO₃/SrTiO₃. La₀.₇Ca₀.₃MnO₃/BaTiO₃ exhibits, by comparison to La₀.₇Ca₀.₃MnO₃/SrTiO₃, more complex reciprocal space maps [Figs. 3(c) and 3(d)]. Figure 3(c) shows two main peaks [labeled (200) and (002)] whose misorientation matches the theoretical value of 90° - 2 atan (a/c) = 0.6° corresponding to 90° domain walls in the T phase.²⁸ At larger L values, two La₀.₇Ca₀.₃MnO₃ peaks are visible corresponding to La₀.₇Ca₀.₃MnO₃ on a and c.
ferroelectric BaTiO$_3$ domains. Their out-of-plane parameters are $c = 3.834$ and 3.852 Å, respectively. This implies a 0.5% difference in the deviation from the pseudocubic symmetry due to the change in the out-of-plane parameter. From the asymmetric reciprocal space map near BaTiO$_3$ ($-103$) + ($-301$) [Fig. 3(d)], we can calculate only a single value for the in-plane parameter, $a = 3.915$ Å, and observe La$_{0.7}$Ca$_{0.3}$MnO$_3$ on BaTiO$_3$ to be partially relaxed ($R \approx 0.7$). As-prepared samples show relaxation varying between $R = 0.3$ to 0.7. From the width of the broad La$_{0.7}$Ca$_{0.3}$MnO$_3$ peaks in the symmetric and asymmetric reflections, we estimate coherence lengths in the out-of-plane direction, $L_c = 70–95$ Å. Coherence lengths in the in-plane direction, $L_a$, fall in a broader interval (70–200 Å, depending on the sample) unrelated to any systematic variation of morphological or structural features. At room temperature, La$_{0.7}$Ca$_{0.3}$MnO$_3$ thin films on BaTiO$_3$ are strained: tensile in-plane and compressive out-of-plane.

B. Magnetism

La$_{0.7}$Ca$_{0.3}$MnO$_3$ thin films on BaTiO$_3$ show interesting magnetic properties: the saturation moments ($M_S$) of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ [Figs. 4(b)–4(d)] are depressed compared to La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ [Fig. 4(a)], whereas the coercive fields are an order of magnitude larger.$^{18}$ A blocking temperature can be defined below the O-R transition in La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$, where the ZFC magnetization has a maximum, as depicted in Figs. 4(b)–4(d). This magnetic behavior was interpreted as a signature of a granular magnetic system in agreement with the linear temperature dependence of the coercive fields.$^{18}$ Rather conspicuously, some La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples exhibit negative magnetization at low temperature after cooling without applied field, see Fig. 4(c). As expected, both Curie temperature ($T_c$, see Fig. 4) and $M_S$ (see Fig. 5) increase with sample thickness: $T_c$(120 Å) = 180 K, $T_c$(150 Å) = 220 K, and $T_c$(240 Å) = 230 K. As previously reported on La$_{0.7}$Sr$_{0.3}$MnO$_3$/BaTiO$_3$ (Refs. 11 and 12), hysteretic jumps of the magnetization are detected around the BaTiO$_3$ phase transitions that become smoother in thick films (Fig. 4 insets). The isothermal behavior, depicted in Fig. 5, reveals that thinner samples (120 Å) have hysteresis cycles with features that resemble Matteucci cycles between 60 and 120 K (Fig. 4 inset for $M_s$ and $H_c$ vs $T$), as previously reported. The magnetization overshoots symmetrically on both branches and involves almost 30% of the moment. This was interpreted on magnetoelastic grounds as due to the existence of a fraction of moments, near the La$_{0.7}$Ca$_{0.3}$MnO$_3$ interface with BaTiO$_3$, whose magnetization aligns out of plane with increasing applied magnetic field. The easy axis remains in plane at all temperatures [Fig. 5(a)]. Thicker samples (150, 240 Å) do not exhibit Matteucci-like features, have saturated moments closer to the bulk values, but still show large coercive fields [Fig. 5(c)]. Figure 6 compares for a 120-Å La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ the hysteresis loops recorded at 190 K after either cooling from 300 K in the BaTiO$_3$ O phase or warming from 10 K in the R phase. Even though the magnetic moment is higher in the R phase, the coercive fields are larger in the O phase, indicating the strong influence of the surface morphology (different in the two phases, as observed in the SPM topographical images) on the magnetic properties of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ film. The observed magnetic moment difference between the two phases at 190 K is compatible with differences stemming either from substrate-induced strain (via magnetoelastic and magnetostrictive coupling) or from electric polarization [via giant converse magnetoelectric coupling with coefficients of the order of magnitude determined for La$_{0.7}$Sr$_{0.3}$MnO$_3$ on BaTiO$_3$ (Ref. 10) and for 300-Å La$_{0.7}$Ca$_{0.3}$MnO$_3$ on relaxor substrate Pb(Mg$_{1/3}$Nb$_{2/3}$)$_{3}$O$_{3}$/PbTiO$_{3}$ (Ref. 30)] or a combination of both.

C. Resistivity

The exotic magnetic behavior of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ shows up in its electronic transport properties. Figure 7 compares the temperature-dependent resistivity of La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and various La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples. There are large differences between La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$...
and La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$. The La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ follows the behavior expected for an optimally doped thin epitaxial manganite layer: there is a metal insulator transition ($T_{MI}$) near the Curie temperature, which shifts towards higher temperature when increasing the applied field.$^{21}$ The resistivity and magnetoresistance are very low at low temperatures with negligible thermal hysteresis.

Thin (120 Å) La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples exhibit two hysteretic jumps, coinciding with the two first-order structural transitions of BaTiO$_3$ at $T_{R-O} = 188$ K (196 K) and $T_{O-R} = 283$ K (293 K) upon cooling (warming).Remarkably, the resistivity variation at the R-O transition, $\Delta \rho_{R-O}$, exceeds two orders of magnitude and overlaps with the usual M-I transition near $T_C$. This resistivity jump is sample dependent, although in most cases, it runs from higher resistance at the high-temperature...
side to lower resistance at the low-temperature side. This is consistent with the typically observed upwards jump of the magnetization as the temperature is lowered. Nevertheless, the sign of $\Delta \rho_{\text{FC}}$ may differ even between simultaneous measurements along the two perpendicular sample edges in the van der Pauw geometry; this is suggestive of the importance of the distribution of ferroelectric domains in BaTiO$_3$ for the conductance pathways which may differ from one sample to another and be further affected by thermal history. Indeed, most thin La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ (120 Å) samples show two metal insulator transitions at around $T_{\text{MI}} = 160$ K and $T_{\text{MI}} = 100$ K, respectively coinciding with the onset of ferromagnetism at $T_C$ and slightly below the blocking of the magnetic system around 120 K. Here, $T_{\text{MI}}$ increases from 160 K in zero magnetic field to above 260 K for an applied field of 8 T [see Fig. 7(b)], a behavior similar to that observed for La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and as expected for the conventional MI transition of optimally doped manganites. This is not the case for $T_{\text{MI}}$. It hardly shifts with field, demonstrating the appearance of a fraction of magnetic moments quite insensitive to the application of an external magnetic field and forming insulating regions. When measuring with field perpendicular to the sample plane, the observed phenomenology is qualitatively the same as with the field parallel to it.

There is a striking hysteretic thermal behavior of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$. Figure 8 shows the temperature dependence of the difference of resistivity ($\Delta \rho$) between warming and cooling runs (note the logarithmic scale). Irreversibilities ($\Delta \rho > 0$) are apparent around both metal-insulator transitions, although they are far more pronounced for the $T_{\text{MI}}$ freezing transition in zero field and, curiously enough, are also strongly enhanced in the paramagnetic region. The latter persists up to the highest fields studied. Also, irreversibilities around $T_{\text{MI}}$ are very sensitive to the application of an external magnetic field. This observation rules out secondary and nonstoichiometric fractions as responsible for the appearance of a second transition at $T_{\text{MI}}$. The R-O BaTiO$_3$ structural transition trivially yields very large $\Delta \rho$ between 188 and 196 K, due to its hysteretic nature.

![Figure 8](image.png)

**FIG. 8.** (Color online) Temperature dependence of thermal resistivity hysteresis ($\Delta \rho$) in selected magnetic fields: 0 T (black), 4 T (blue), and 8 T (green).

**D. Magnetoresistance**

The isothermal magnetoresistance (MR) also reveals important differences between La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$. Figure 9 shows the field-dependent MR at several temperatures for 120-Å thick La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$. Colossal MR ratios are observed at temperatures near $T_C$ as expected in optimally doped manganites. For thin (120 Å) La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$, large and hysteretic MR is observed at low temperatures that is absent in either La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ or thicker La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$. Again, hysteretic behavior, this time with applied field, is observed for the thin La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ over a broad temperature range. For temperatures above $T_{\text{MI}}$, hysteresis is also present in La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$, as expected from the percolative nature of the transition. The MR of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ remains large at low temperature, indicating lack of complete magnetic ordering. This is in agreement with the granular magnetic behavior exhibited below the freezing temperature.

![Figure 9](image.png)

**FIG. 9.** (Color online) Magnetoresistance of (a) La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and (b) La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ at selected temperatures (thickness: 120 Å in the two cases).

**E. Poling**

To explore the role of ferroelectric BaTiO$_3$ domains in the magnetic and electronic properties of La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$, we study the effect on the film resistivity of
electrically poling the substrate at room temperature. Figure 10 shows the resistivity of a thin (120 Å) film before and after BaTiO₃ poling. Upon cooling after poling, the peak at $T'_{MI}$ remains, while the transition at $T_{MI}$ is practically obscured by the change induced by the O-R structural transition. The low-temperature resistivity increases an order of magnitude after poling and thermal hysteresis is strongly enhanced. Note also the sign change of $\Delta \rho$ upon approaching the O-R transition from below. In spite of this hysteretic behavior, the high-temperature resistance remains unchanged, assuring the reproducibility of the current paths (i.e., lack of fractures). In thicker La₀.₇Ca₀.₃MnO₃/BaTiO₃, the effect of the BaTiO₃ morphology on transport properties can also be appreciated: the resistivity around the O-R transition is dramatically altered upon poling (inset to Fig. 10), even though $T'_{MI}$ was not seen either before or after poling.

**F. Electroresistance**

A complementary phenomenon to magnetoresistance, electroresistance, refers in its broadest sense to any nonlinear current-voltage characteristics. Figure 11 shows the voltage-dependent normalized resistivity $R/R_0$ curves (where $R_0$ is low bias resistance) at selected temperatures for 120-Å-thin films of La₀.₇Ca₀.₃MnO₃/SrTiO₃ and La₀.₇Ca₀.₃MnO₃/BaTiO₃. Contrary to the La₀.₇Ca₀.₃MnO₃/SrTiO₃ case, where it is negligible, ER in La₀.₇Ca₀.₃MnO₃/BaTiO₃ is significant and nontrivial. For the former, the resistance is either ohmic (linear, e.g. at 200 K) or decreases slightly ($\Delta R/R_0 < 1\%$, e.g. at 100 K and the low-voltage part at 10 K). The increase of resistance with voltage in La₀.₇Ca₀.₃MnO₃/SrTiO₃ (e.g. at 10 or 140 K) is a mere consequence of Joule heating in the metallic regime. This extreme was also checked with pulsed measurements at certain temperatures. Electroresistance in La₀.₇Ca₀.₃MnO₃/BaTiO₃ reaches 20% at $T = 150$ K and $V = 1$ V. Once again, the upturn of $R/R_0$ for $V > 1$ V is a consequence of Joule heating and is not considered in our analysis. In order to quantify these data, we define the ER threshold voltage $V_\text{th}$ as the voltage where $R$ departs from ohmic behavior [as illustrated in Fig. 11(b)], and ER as $\Delta R/R_0 = (R(V) - R_0)/R_0$ for $V = 2V_\text{th}$. We summarize these data in Figs. 12(a) and 12(b) showing the temperature dependence of threshold voltage $V_\text{th}$ and ER, respectively. The threshold voltage has a broad dip centered around $T \approx 130–160$ K, coinciding with the strongest ER. These salient changes of ER and threshold voltage occur in the temperature range where anomalies in the magnetic hysteresis cycles are observed and also near $T_{MI}$. Note that the rather small magnitude of ER (up to 4%) is only due to our operational definition of ER, taken at $V = 2V_\text{th}$. To summarize our electroresistance experiments, La₀.₇Ca₀.₃MnO₃/BaTiO₃ shows very steep and large resistance drop above threshold up to $T_{MI}$, as opposed to La₀.₇Ca₀.₃MnO₃/SrTiO₃, which barely displays a temperature-dependent ER.

**IV. DISCUSSION**

From the structural and topographic data, the following picture of La₀.₇Ca₀.₃MnO₃/BaTiO₃ emerges. The films are epitaxial with structural coherence volumes on the order of $(70–90) \times 200 \times 200$ Å$^3$ and characterized by a biaxial strain largely compressive out of plane and tensile in plane. The strained La₀.₇Ca₀.₃MnO₃ film adjusts to the lattice changes experienced by BaTiO₃ upon cooling, heating, or poling, exhibiting hysteretic behavior at the BaTiO₃ phase transitions. Since through these phase transitions the two tetragonal lattice constants of the substrate eventually merge into a single value corresponding to the rhombohedral lattice constant (see Fig. 1 and Table I), we assume the La₀.₇Ca₀.₃MnO₃ layer to elastically smear out any strain differences between...
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FIG. 12. (Color online) (a) Threshold voltage and (b) electroresistance for $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/SrTiO$_3$ (black solid squares) and $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/BaTiO$_3$ (blue open circles) as a function of temperature.

$\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$ cells on ferroelectric domains in the T and O phases. This assumption can only be validated in part by our low-temperature structural study: the observed $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$ peak exhibits a single maximum, but it is substantially broad. On the basis of our SPM observations, we expect multiple FE domains in our BaTiO$_3$ substrates. These domains will be arranged in patterns determined largely by the ferroelectric-elastic equilibrium reached in the bulk at each temperature with only minimal contributions from the depolarizing field introduced by the changing conduction properties of the $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$ layer. Thus, it is necessary to discuss the properties exhibited by the $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$ thin films in terms of the structural changes experienced by the BaTiO$_3$ substrate, since the layer remains epitaxial. The limited coherence (70–90 Å) in the out-of-plane direction is consistent with a corrugated $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/BaTiO$_3$ interface. In the T phase of BaTiO$_3$, a characteristic corrugation angle of 0.6° is introduced by 90° domain walls. Upon cooling BaTiO$_3$ substrates through the O phase, the topography and diffraction pattern introduced by the new FE domain structure is not significantly different from that of the T phase. In contrast, the transition to the R phase introduces a secondary corrugation (there is good agreement between the experimental values for the corrugation angle determined from SPM and x-ray diffraction), which only becomes stable at 100 K, within the time required for SPM imaging. Recent results with a phenomenological Ginzburg–Landau–Devonshire model predict 71° and 109° domain walls in the R phase to be as thin and stable as the 180° domain walls in the T phase. Note that with 109° domain walls, the expected corrugation by reflection twinning in (001) R planes is $2^\circ(90 - \alpha) = 0.3°$, where $\alpha$ is the rhombohedral angle. The presence of both corrugations makes the morphology of the BaTiO$_3$ surface in the R phase more fine grained, introducing a new characteristic length scale (in the micron range). Consequently, we have experimental and theoretical support for added phenomenology for $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$ on rhombohedral BaTiO$_3$ with respect to higher temperatures.

This complex structure has a strong influence on the magnetic properties of thin $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/BaTiO$_3$ (120 Å):

1. Firstly, the Curie transition is broadened, the coercive field is one order of magnitude larger than in the reference $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/SrTiO$_3$, and a clear anomaly appears in the temperature-dependent magnetization below the O-R transition, indicating magnetic moment blocking or freezing and granular magnetic behavior.

2. Secondly, almost half of the expected 3.7 $\mu_B$/Mn magnetic moments are missing and do not orient even at low temperature and high field (5 T) implying that an important fraction of magnetic moments are not participating in long-range FM order. These show up actively in the anomalous Matteucci-like hysteresis loops, as well as in the enhancement of the out-of-plane saturation moment in high field. On magnetoelastic grounds, Matteucci-like cycles have been shown to be consistent with the existence of an out-of-plane spin population (amounting to approximately 1/3 of the available spins) that is moderately sensitive to magnetic field. Thicker $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/BaTiO$_3$ films hardly show missing magnetic moment, but their coercive fields are much larger than those of the reference $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/SrTiO$_3$. The observation of depressed magnetic moment could also be compatible with AFM behavior below its spin-flip field coexisting with in-plane FM regions.

3. Thirdly, negative magnetization (i.e. opposing the applied field) is observed in low fields at low temperature in certain samples. This behavior is characteristic of frozen AFM correlations in a frustrated system.

Magnetotransport properties are extremely sensitive to changes in double-exchange interactions, which are in turn strongly affected by the variations in the angles between MnO$_6$ octahedra induced by strain or by changes in the crystal field. Unlike in $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/SrTiO$_3$ and bulk $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$, $\text{La}_0.7\text{Ca}_0.3\text{MnO}_3$/BaTiO$_3$ thin films (120 Å) show two well-defined MI transitions. Here, $T_M$ is described as the usual metal-insulator transitions in FM perovskite manganites: insulating clusters intermixed into the long-range conducting FM order grow with increasing temperature, and electronic transport becomes dominated by electronic percolation through FM regions. Above $T_c$, the usual paramagnetic insulating ordering appears. A magnetic field strengthens the FM clusters and shifts the transition to higher temperature. However, the second transition, $T_{MI}^\prime$, does not fit this picture as the magnetic field does not shift this transition temperature. This suggests that the clusters responsible for this $T_{MI}^\prime$ are not affected by the magnetic field, unlike the paramagnetic regions in the usual MI transition. The considerable magnetoresistance is then due to the interface between small FM and non-FM regions. Irreversibility between cooling and warming is usually considered a signature of the percolative nature of the transition. Around $T_M$ the phase-separation balance changes, favoring the insulating non-FM clusters. Structural changes of the substrate, evolution of the surface morphology, drive the competition between phases, and this translates to a highly hysteretic MI transition.
Although, most of our experimental data can be interpreted solely on the basis of the purely FM order with spatially inhomogeneous anisotropy (coexisting regions of in-plane and out-of-plane FM interaction), other ingredients may play a role. Hints come from the negative magnetization measured in the ZFC of some samples and the hard and insulating behavior of the spins responsible for $T_{\text{MI}}$. We propose that AFM correlations could be enhanced in La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ close to the BaTiO$_3$ interface beyond the level expected in optimally doped bulk and thin film manganites (and that should be also present to a much lesser extent in La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$ and thicker La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples). In this picture, La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ thin films consist of FM regions interspersed with AFM ones, with strong magnetic frustration at their boundaries.

What would be the origin of this enhancement of AFM interactions in an optimally ($x = 0.3$) doped manganite thin film? We first consider tetragonal distortion induced by strain which affects orbital ordering. Indeed, for La$_{1−x}$Sr$_x$MnO$_3$ (Ref. 37), the phase diagram calculated from first principles show the stability region of the FM order to be largely reduced: for $x = 0.3$ doping in La$_{0.7}$Sr$_{0.3}$MnO$_3$, $c/a < 0.96$ corresponds to AFM order. For our La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples, the $c/a$ ratio for La$_{0.7}$Ca$_{0.3}$MnO$_3$ can be estimated in the R phase of BaTiO$_3$ from synchrotron x-ray diffraction, giving $c/a = 0.98$ at 132 K (Ref. 18), implying FM order. However, in line with the magnetoelastic model proposed in Ref. 18, we may assume that the cells of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ layer lying close to BaTiO$_3$ are severely strained with in-plane lattice parameters of BaTiO$_3$. Under this hypothesis, the tetragonality ratio would be $c/a = 0.94$, making the presence of AFM order plausible close to the interface.

Secondly, recent ab initio and two-orbital model calculations explore the effect of the electric polarization of the FE on the magnetic state of manganite in connection with manganite/FE/manganite heterostructures. They conclude that interfacial spins, under various FE polarization scenarios, switch to non-FM arrangements, most of them concerning AFM coupling. In films thicker than a few atomic layers, AFM arrangements would therefore coexist with FM arrangements, giving rise to phase separation, similar to that observed in bulk La$_{0.7}$Ca$_{0.3}$MnO$_3$ (Ref. 20). These effects predominate near the FM/FE interface over only a few unit cells, so the associated phenomenology blurs out in thicker films, akin to our observations.

With either the strain or electric-field-induced AFM mechanism, transport properties of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ layer will be very sensitive to the electric poling of the BaTiO$_3$ substrate. In these conditions, magnetoelastic effects are expected, changing the equilibrium between the manganite microphases from that corresponding to a random polarization distribution. We observe precisely this (Fig. 10): upon poling, the resistance near $T_{\text{MI}}$ increases, whereas the usual MI transition is depleted, showing that a larger fraction of the La$_{0.7}$Ca$_{0.3}$MnO$_3$ could be in an AFM state. In the R phase, the polarization lies along the unit cell diagonals. A poling process perpendicular to the sample surface at room temperature enhances the formation of larger domains oriented parallel to the applied electric field. When cooling to the R phase, these FE domains remain with a large net component of polarization in the poling direction. These domains can act as nucleation centers for the AFM patches. As the new FM and AFM magnetic domains develop simultaneously with decreasing temperature due to the new pattern of FE domains, no exchange bias in the hysteresis cycles is expected (indeed none is observed). BaTiO$_3$ O-R transition would enhance phase separation. It is difficult to ascertain on quantitative grounds whether this behavior would be the same if an out-of-plane fraction of spins were enhanced upon poling. Note that despite the very high magnetic fields applied, it has been impossible to achieve alignment of the out-of-plane moments. This behavior would imply unusual and extremely high out-of-plane anisotropy values.

Whatever is the etiology of the unruly moment fraction, our model naturally leads to a granular metallic system, confirmed by the high resistivity and large magnetoresistance at low temperatures. Also, electroresistance is sensitive to conduction pathways and the associated distribution of potential barriers and thus is a good measure of electric inhomogeneity. Electroresistance is two orders of magnitude larger in La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ at low temperature than in La$_{0.7}$Ca$_{0.3}$MnO$_3$/SrTiO$_3$, doubling further to a maximum around 140 K with a concomitant minimum of the threshold voltage (see Fig. 12). This again could point to a dramatic increase in the activation energies triggered by an enhancement of the AFM order well below both the O-R BaTiO$_3$ transition and $T_{\text{MI}}$.

The anomalous phenomenology found in the 60–150 K temperature range seems to be linked to the secondary corrugation introduced by ferroelectric domain walls and developing in the BaTiO$_3$ substrate below 180 K. These changes in morphology are a signature of changes in the characteristic lengths for strain and electric polarization fields and, given the strong interplay between structural, electronic, and spin degrees of freedom and electrostatic boundary conditions in La$_{0.7}$Ca$_{0.3}$MnO$_3$, necessarily affect the magnetism of La$_{0.7}$Ca$_{0.3}$MnO$_3$ near the interface. From our results, it is not possible to establish unambiguously the relative importance of strain, geometric, and electrostatic factors, and further experimental work is needed in this direction. However, it should be noted that: (i) within the R phase of BaTiO$_3$, thermal lattice constant variations do not exceed 0.05% (Ref. 25); (ii) while primary corrugation has a characteristic length in the 15–μm range, secondary corrugation reduces this magnitude by a factor of 2; and (iii) the magnetic and transport anomalies are not present in thicker La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ samples. From (i), we can conclude that homogeneous in-plane strain effects cannot play a major role in causing the observed phenomenology; from (ii), we can expect a twofold increase in the rate of alternation of the sign of spontaneous electrostatic polarization of the La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ interface by the substrate with its associated changes in La$_{0.7}$Ca$_{0.3}$MnO$_3$ electronic and spin degrees of freedom; from (iii), a vertical gradient is a plausible option for the spatial distribution of the anomalies. We propose that, between 180 and 100 K and triggered by the O-R BaTiO$_3$ phase transition, La$_{0.7}$Ca$_{0.3}$MnO$_3$/BaTiO$_3$ experiences a renormalization of the existing delicate equilibrium between intrinsic phases that was developing below $T_{\text{MI}}$. These effects are overcome when ferromagnetism starts to be the dominant phase and smoothly pervades the system as the
temperature is lowered below 60 K. It is in this temperature range where Lao.7Ca0.3MnO3/BaTiO3 is most sensitive to external magnetic fields (colossal magnetoresistance) or strain (shift in TMI), due to the almost degenerate structural, electronic, and spin degrees of freedom. Therefore, prior to reaching a robust FM state, below 60 K in our case, the system could be particularly prone to developing AFM phases, induced by external perturbations such as those induced by the evolving secondary corrugation. This is in line with previously reported experiments in Lao.7Ca0.3MnO3 150-A-thin films deposited on LaAlO3 where the existence of a charge order insulating phase at low temperatures has been demonstrated18 and correlated to the existence of large inhomogeneous strains induced during the thin layer growth process. In 50-A Lao.7Ca0.3MnO3 on SrTiO3 (Ref. 39), under uniform strain conditions, magnetic and transport measurements have been interpreted on the basis of the existence of an AF insulating phase which occupies nearly 70% of the film.

V. CONCLUSIONS

We have shown magnetic and transport property anomalies to be present around 60–150 K in Lao.7Ca0.3MnO3/BaTiO3 thin films. An extra resistance peak appears around 120 K that is quite insensitive to magnetic field and is accompanied by a strong increase of the electroresistance. Thin Lao.7Ca0.3MnO3/BaTiO3 films behave as a magnetic and metallic granular system, albeit they are structurally epitaxial. The anomalies disappear with increasing Lao.7Ca0.3MnO3 thickness, suggesting a vertically segregated structure. We have argued that the evolving surface morphology of the ferroelectric BaTiO3 substrate and its associated strain and electric field changes could enhance phase separation between AFM and FM local order in the Lao.7Ca0.3MnO3 layer, in line with current theoretical studies. However, an alternative explanation based solely on coexisting in-plane and out-of-plane FM populations cannot be ruled out. The magnetic/metallic granularity and all anomalies can be explained by the intimate mixing of AFM and FM regions or, alternatively, in-plane and out-of-plane FM patches. A neat magnetoelectric coupling is apparent upon poling, and probably both strain and electron doping effects are at the root of our observations.

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